Research Article



## More on the bounds for the skew Laplacian energy of weighted digraphs

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**Abstract:** Let  $\mathscr{D}$  be a simple connected digraph with *n* vertices and *m* arcs and let  $W(\mathscr{D}) = (\mathscr{D}, w)$  be the weighted digraph corresponding to  $\mathscr{D}$ , where the weights are taken from the set of non-zero real numbers. Let  $\nu_1, \nu_2, \ldots, \nu_n$  be the eigenvalues of the skew Laplacian weighted matrix  $\widetilde{SLW}(\mathscr{D})$  of the weighted digraph  $W(\mathscr{D})$ . In this paper, we discuss the skew Laplacian energy  $\widetilde{SLEW}(\mathscr{D})$  of weighted digraphs and obtain the skew Laplacian energy of the weighted star  $W(\mathscr{K}_{1,n})$  for some fixed orientation to the weighted arcs. We obtain lower and upper bounds for  $\widetilde{SLEW}(\mathscr{D})$  and show the existence of weighted digraphs attaining these bounds.

**Keywords:** Weighted digraph, skew Laplacian matrix of weighted digraphs, skew Laplacian energy of weighted digraphs

AMS Subject classification: 05C30, 05C50

## 1. Introduction

A weighted digraph  $W(\mathscr{D})$  (or a weighted network) is defined to be an ordered pair  $(\mathscr{D}^u, w)$ , where  $\mathscr{D}^u = (V, \mathscr{A})$  is the underlying digraph of  $W(\mathscr{D})$  and  $w : \mathscr{A} \to \mathbb{R} - \{0\}$  is the weight function. Weight of any arc e = (u, v) is denoted by w(e). Every digraph can be regarded as the weighted digraph with weight of each arc equal to one.

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